

## Problem Set 3 Recursion Theory

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**Due September 28, 2005**

[CT] is *Computability Theory* by Barry Cooper.

1. **Exercise 2.4.11, pg. 39** Write a Turing program for the function  $g(x, y) = x \dot{-} y$ .
2. Show that if  $f : \mathbb{N} \rightarrow \mathbb{N}$  is *TM*-computable then there are infinitely many *TM*-programs that compute  $f$ .
3. Show that if  $h : \mathbb{N} \times \mathbb{N} \rightarrow \mathbb{N}$  is *TM*-computable, then  $f(n) = \mu z.[h(m, z) = 0]$  is also *TM*-computable.